

Notes 7.3 – Periodic Graphs

Identify the parts of the periodic graph:

$$y = a \sin(b\theta) + d$$

← vertical shift
 ↑ determines period
 → amplitude

Finding the value of b: $\frac{360^\circ}{b} = \text{period}$ or $b = \frac{360^\circ}{\text{period}}$

- a. Write the equation for a sine graph with an amplitude of 3, a period of 180°, and a vertical shift down 1.

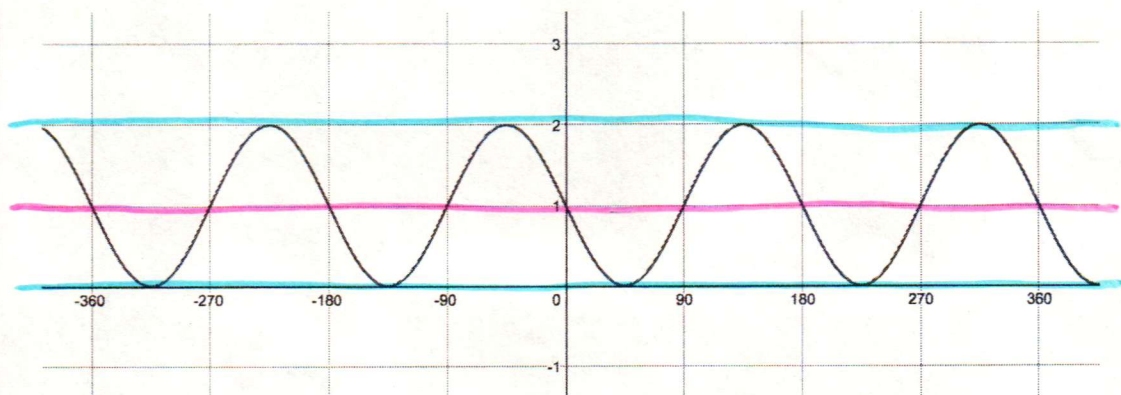
Equation: $y = 3 \sin(2\theta) - 1$

- b. Write the equation for a cosine graph with an amplitude of 2, a period of 120°, and a vertical shift up 1, and is reflected over the center.

Equation: $y = -2 \cos(3\theta) + 1$

Identify the values in the graph and then write the equation that would create the given graph.

c.



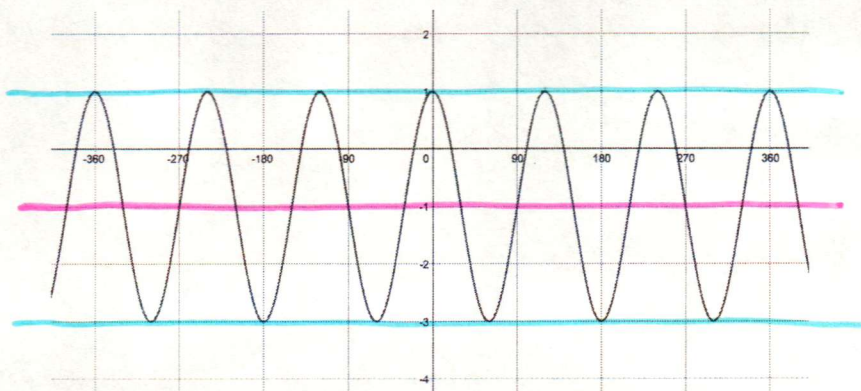
Amplitude: 1

Vertical Shift: +1

Period: 180°

Equation: $y = -\sin(2\theta) + 1$

d.



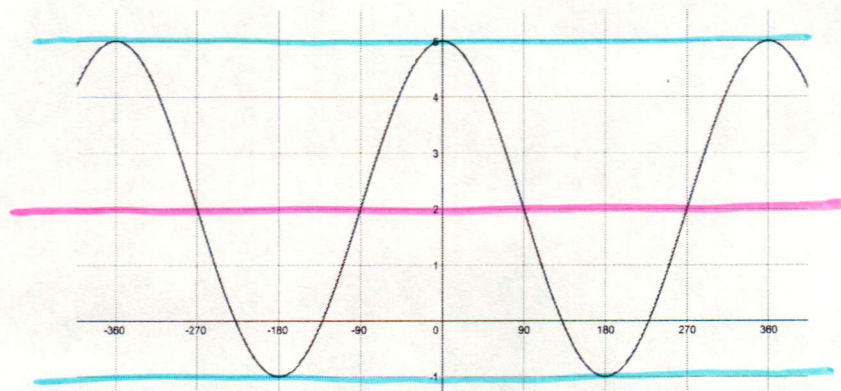
Amplitude: 2

Vertical Shift: -1

Period: 120°

Equation: $y = 2 \cos(3\theta) - 1$

e.



Amplitude: 3

Vertical Shift: +2

Period: 360°

Equation: $y = 3 \cos \theta + 2$

Looking at the unit circle:

$$0^\circ = 0\pi$$

$$90^\circ = \frac{\pi}{2}$$

$$180^\circ = \pi$$

$$270^\circ = \frac{3\pi}{2}$$

$$360^\circ = 2\pi$$

Graphing using Radians – Equations with radians use x instead of θ

Finding the period with radians: $\frac{2\pi}{b} = \text{period}$

$b = 2$

period = $\frac{2\pi}{2} = \pi$

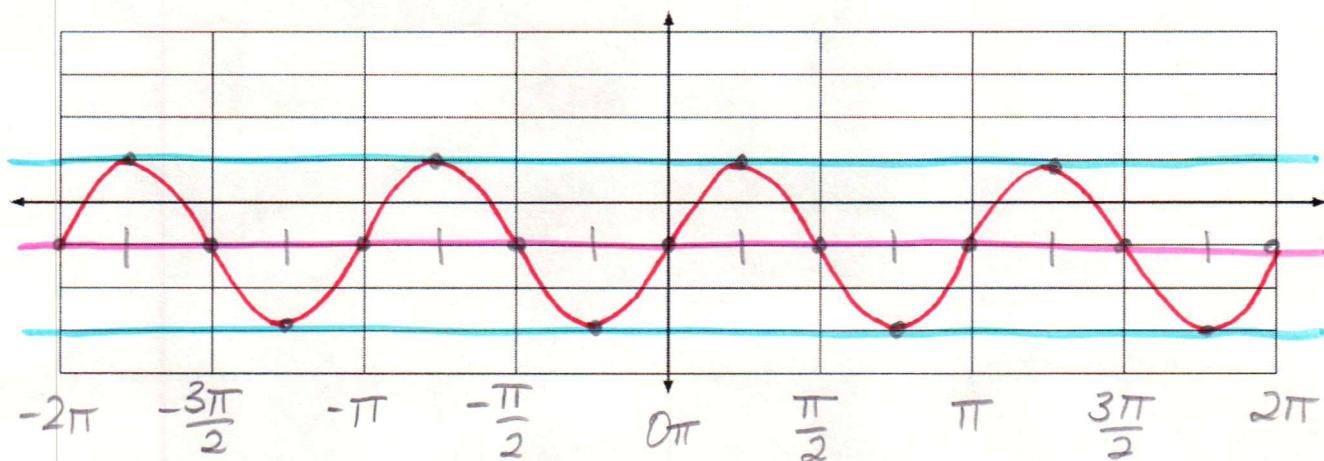
$b = 3$

period = $\frac{2\pi}{3}$

$b = 4$

period = $\frac{2\pi}{4} = \frac{\pi}{2}$

Graph $y = 2 \sin(2x) - 1$

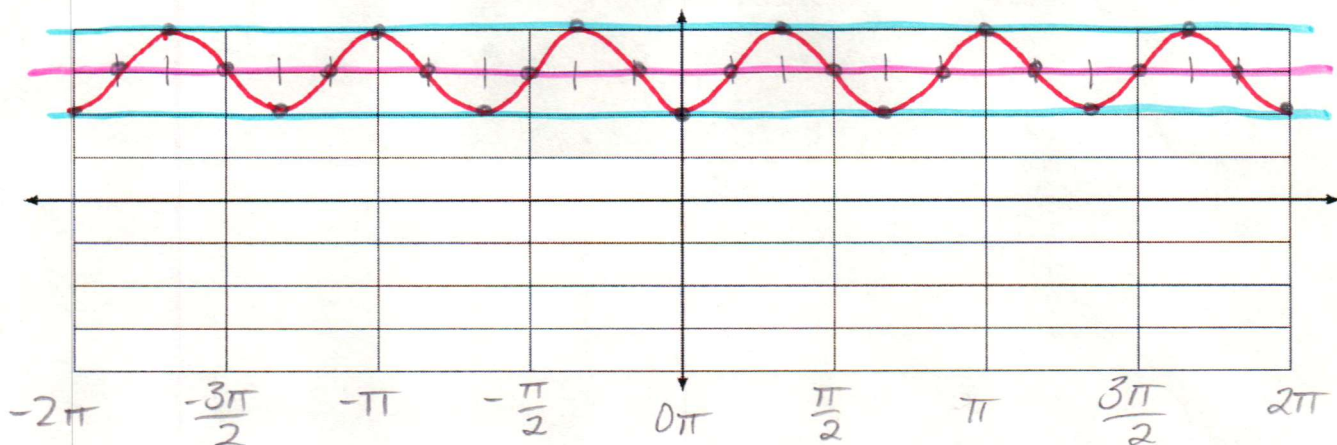


Amplitude: 2

Vertical Shift: -1

Period: π

Graph $y = -\cos(3x) + 3$



Amplitude: 1

Vertical Shift: +3

Period: $\frac{2\pi}{3}$